Rossmoyne Senior High School

Semester One Examination, 2018

Question/Answer booklet

MATHEMATICS APPLICATIONS UNIT 3 Section One: Calculator-free	SOLUTIONS
Student number:	In figures
	In words
	Your name
Time allowed for this se Reading time before commencin Working time:	
Materials required/reco To be provided by the superv This Question/Answer booklet Formula sheet	ommended for this section

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	10	10	100	98	65
				Total	100

Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- 3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

2

Section One: Calculator-free

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

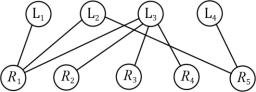
Working time: 50 minutes.

Question 1

(b)

(5 marks)

Four university lecturers $(L_1, L_2, L_3 \text{ and } L_4)$ have been allocated five rooms $(R_1, R_2, R_3, R_4 \text{ and } R_5)$ to teach in. Only one lecturer will teach in a room at any time. Because some of the lecturers require specialist equipment, not all the rooms can be used by all the lecturers, as shown in the graph below.



(a) What is the name of such a graph shown above, where the vertices can be split into two groups so that each edge joins a vertex from one group to a vertex in the other group?

(1 mark)

 Solution

 Bipartite

 Specific behaviours

 ✓ correct name

Solution

Specific behaviours correct number

3 lecturers.

(1 mark)

(1 mark)

(c) How many rooms can lecturer L_3 use?

How many lecturers can use room R_1 ?

Solution
4 rooms.
Specific behaviours
✓ correct number

- (d) Briefly explain whether
 - (i) all the rooms could be in use at the same time?

(1 mark)

Solution
No - not enough lecturers.
Specific behaviours
✓ no, with valid reason

(ii) all the lecturers can teach at the same time?

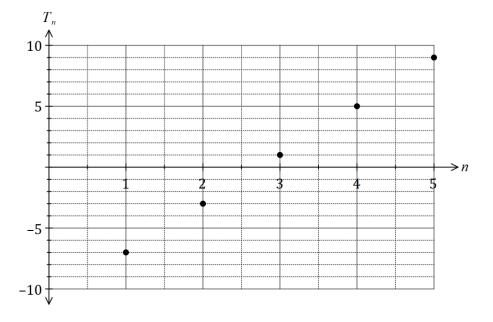
(1 mark)

Solution
No - L_1 , L_2 and L_4 can only use R_1 and R_5 .
Specific behaviours
✓ no, with valid reason

3

(4 marks)

The first five terms of an arithmetic sequence are shown on the graph below.



4

(a) Deduce a rule for the n^{th} term of this sequence.

Solution $T_n = -7 + (n - 1)(4)$ = 4n - 11Specific behaviours \checkmark identifies common difference \checkmark rule (accept any correct form)

(b) Given that the k^{th} term of this sequence is 1 197, determine the value of k. (2 marks)

Solution

$$-7 + (k - 1)(4) = 1197$$

$$(k - 1)(4) = 1204$$

$$k - 1 = \frac{1204}{4} = 301$$

$$k = 302$$
Specific behaviours
 \checkmark uses equation from (a)
 \checkmark solves for k

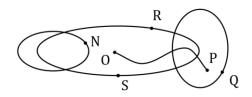
(2 marks)

5

Question 3

(7 marks)

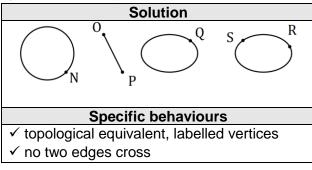
Graph G_1 is shown below, with vertices N, O, P, Q, R and S.



(a) In graph theory, a planar graph is a graph that can be drawn in the plane. Describe how to draw the edges of such a graph to clearly show that it is planar. (1 mark)

Solution
Draw so that no two edges cross, or, draw so
that edges only meet at vertices.
Specific behaviours
✓ description

(b) Redraw graph G_1 to clearly show that it is planar.



 $2 \log n$

(c) State the number of loops graph G_1 contains.

(1 mark)

(2 marks)

Specific behaviours
✓ number of loops

Solution

(d) Show that Euler's formula does not apply to graph G_1 .

(3 marks)

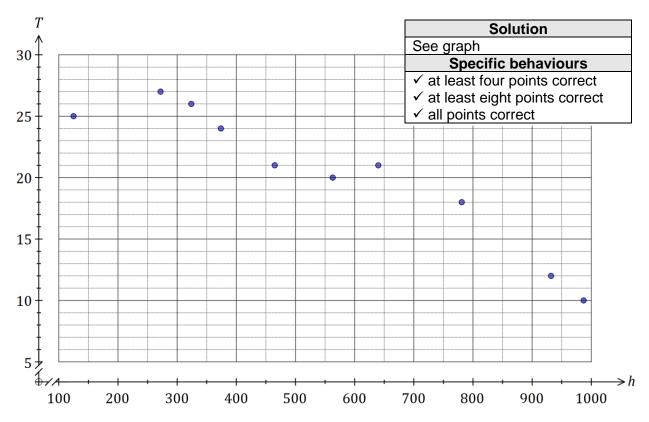
Solution
f = 4, v = 6, e = 5
f + v - e = 4 + 6 - 5 = 5
Hence Euler's formula does not apply as result should be 2, not 5.
Specific behaviours
\checkmark correct f, v, e
✓ substitutes into formula
\checkmark indicates that result is not 2

(8 marks)

The average maximum temperature, T °C, was recorded for ten weather stations, together with the altitude of the station, h metres. The data is shown in the table below.

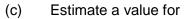
Altitude, h	987	932	781	640	563	465	374	324	272	125
Temperature, T	10	12	18	21	20	21	24	26	27	25

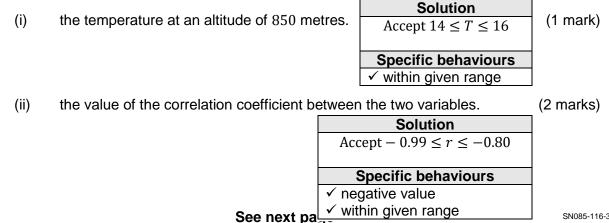
(a) Construct a scatterplot on the axes below that can be used to identify whether an association exists between altitude and temperature. (3 marks)



Describe the features of the scatterplot that indicate a strong, negative and linear (b) association exists between altitude and temperature. (2 marks)

Solution
Strong & linear: points lie close to a straight line
Negative: as altitude increases, the temperature decreases
Specific behaviours
✓ strong & linear reason
✓ negative reason

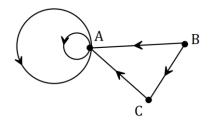




6

(7 marks)

A digraph is shown below.



- (a) State, with justification, whether the digraph contains
 - (i) a walk of length 8.

Solution
Yes. Start at A and travel around a loop 8 times.
Specific behaviours
✓ states yes
✓ lists example walk or other justification

(ii) a Hamiltonian path.

Solution	
Yes. The path is BCA.	
Specific behaviours	
Specific behaviours ✓ states yes	

(b) Using column and row headings in the order A - B - C, construct the adjacency matrix M for the digraph and explain what the number in the third row and first column of matrix M^4 represents. (3 marks)

Solution
$M = \begin{bmatrix} 2 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}$ $M_{3,1}^4$ is the number of ways to travel from <i>C</i> to <i>A</i> along 4 edges.
Specific behaviours
\checkmark at least two rows of <i>M</i> correct
✓ M correct
\checkmark states start, finish vertices and edges used

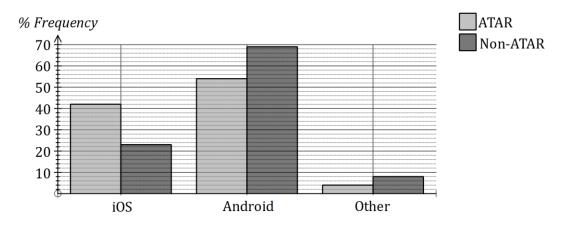
(2 marks)

(2 marks)

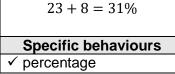
(6 marks)

Mobile phone users who responded to a survey were asked which type of operating system their current phone used (Android, iOS or other) and whether they followed an ATAR or non-ATAR pathway at school. A breakdown of the results is shown in the graph below.

8



(a) What percentage of the respondents who followed a non-ATAR pathway had a phone that did not use Android? **Solution** (1 mark)



- (b) Assuming that the survey results apply to the population in general,
 - (i) does knowing the operating system of a person's phone help you know the pathway they followed at school? Explain your answer. (2 marks)

Solution		
Yes. iOS users were twice as likely to follow an		
ATAR pathway whereas Android and Other users		
were more likely to follow a non-ATAR pathway.		
Specific behaviours		
✓ indicates yes		
✓ explanation		

(ii) does knowing the pathway a person followed at school help you know the type of operating system their phone has? (1 mark)

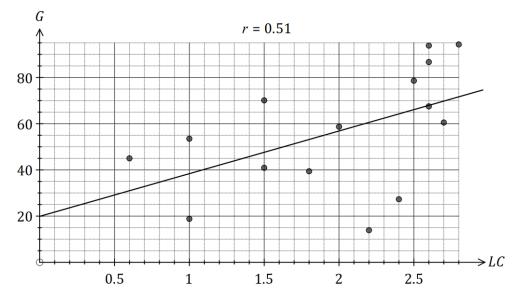
	Solution
Yes.	
	Specific behaviours
✓ indicates yes	

(iii) is there an association between a person's school pathway and type of operating system their phone has? Explain your answer. (2 marks)

Solution		
Yes. If you know the category a person is in for one		
variable, it helps place the person in a category for the		
other variable and so there is an association.		
Specific behaviours		
✓ states yes		
✓ explanation		

(7 marks)

A medical study measured the lipoprotein-cholesterol (LC) and ghrelin (G) levels of a group of patients. The results were displayed in the scatterplot below, together with the least-squares line of best fit and the correlation coefficient between the variables.



How many patients in the study with a lipoprotein-cholesterol level of more than 0.75 had (a) a ghrelin level of less than 65? (1 mark) Solution

8 patients
Specific behaviours
✓ correct number

G between 35 and 65.

Specific behaviours

- (b) Determine the upper and lower predicted ghrelin levels for patients with lipoproteincholesterol levels between 0.8 and 2.45. (2 marks) Solution
- \checkmark lower bound, \checkmark upper bound (c) Comment on the claim that a high lipoprotein-cholesterol level causes a patient to have a high ghrelin level.

(2 marks)

Solution
The claim is not valid. An observed association does not
mean there is a causal relationship between the variables.

Specific behaviours

✓ indicates claim not valid

✓ comments on causality

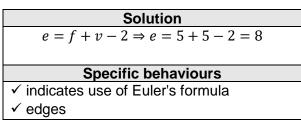
(d) State the number of patients in the study and comment on how the size of the study could influence any explanation for an association between the variables. (2 marks)

1
Solution
There were 15 patients in the study. This is small number
and increases the chance that any association observed
may simply be due to coincidence.
Specific behaviours
✓ number in study
✓ comment linking small samples to unreliable outcomes

APPLICATIONS UNIT 3 Question 8

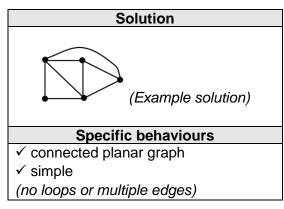
A connected planar graph G_2 has five faces and five vertices.

(a) Determine the number of edges graph G_2 has.



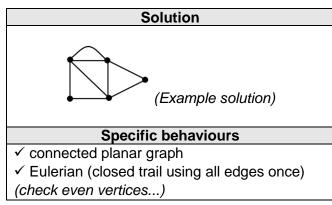
10

- In each of the following, use the additional condition only within that part of the question. (b)
 - (i) Draw graph G_2 so that it is simple.



Draw graph G_2 so that it contains a Eulerian trail. (ii)

✓ connected planar graph



Draw graph G_2 so that it contains a Hamiltonian path but not a Hamiltonian cycle. (iii)

Solution

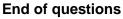
Specific behaviours

✓ semi-Hamiltonian (open path thru' all vertices once)

(Example solution)

(2 marks)

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(8 marks)

CALCULATOR-FREE

(2 marks)

(2 marks)

(2 marks)

Supplementary page

Question number: _____

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